## Golden Threads

- There are six key areas of study throughout - Number, Algebra, Ratio and Proportion, Geometry and Measure, Probability, and Statistics. Whilst these areas can appear distinct, students are encouraged to see the connections across mathematical ideas. We also look to develop their fluency, mathematical reasoning and competence in solving increasingly sophisticated problems.


## Enrichment

- UKMT Junior Maths Challenge
- Weekly puzzle club
- Careers links


## Review and Evaluation

July 2024

| Topics \&t <br> Substantive Knowledge | Assessment | Misconceptions | Key Vocabulary | Knowledge Tracking |
| :---: | :---: | :---: | :---: | :---: |
| Sequences <br> Rather than rushing to find rules for nth term, this topic explores sequences in detail using both diagrams \& lists of numbers: <br> - Describe \& continue a sequence given diagrammatically <br> - Recognise the difference between linear \& non-linear sequences <br> - Generate terms of a sequence from a term-to-term rule | End of Term 1 - In class, 45 minute assessment on the first three blocks of learning. | Students may confuse the coefficient of n with the constant term in the nth term rule. <br> Students may use a positive n when the sequence is decreasing. | Ascending Commutative Descending Equation Evaluate Expression Geometric Identity Inverse Linear Non-linear Operation Substitute Variable | Already Seen: <br> In KS2 students should <br> - recognise, describe and generate linear number sequences and find the term-to-term rule. <br> - use simple formulae <br> - express missing number problems algebraically <br> - find pairs of numbers that satisfy an equation with two unknowns - enumerate possibilities of combinations of two variables. <br> To Build Towards: <br> Year 7 Term 3/4 - substituting \& solving more complex equations, incl. with negative numbers <br> Year 8 Term 3 - More complex nth term rules) |
| Algebraic Notation <br> The focus of this topic is developing a deep understanding of the basic algebraic forms. Function machines are used alongside bar models \& letter notation. <br> - Substitute values in expressions, rearrange \& simplify expressions <br> - Use \& interpret algebraic notation <br> - Generate sequences given an algebraic rule <br> - Represent one and two-step functions graphically |  | Believing that a letter can only stand for one particular number, different letters must stand for different numbers or letters can only stand for whole numbers. <br> Confusing the variable, x with the operation, x . |  |  |
| Equality and Equivalence <br> In this topic students are introduced to forming and solving one-step-linear equations, building on their study of inverse operations. <br> - Use diagrams \& letters to generalise number operations <br> - Understand \& use fact families, numerically \& algebraically <br> - Simplify \& manipulate algebraic expressions by collecting like terms |  | Treating unlike terms as if they are like terms. <br> Misunderstanding of what the equal sign represents: equality Vs do something. |  |  |

## Topics $\subset$ t <br> Substantive Knowledge

## Place value and ordering numbers

In this unit students will explore integers up to one billion \& decimals to hundredths. Using \& understanding number lines is a key strategy explored in depth:

- Understand \& use place value for decimals, measures \& integers of any size
- Order positive \& negative integers, decimals \& fractions
- Round numbers to an appropriate degree of accuracy
- Find the Range \& the Median of a set of numbers
- Interpret \& compare numbers in standard form (H)


## Fraction, decimal and percentage equivalence

Building on the recent work on decimals, the key focus for this topic is for students to gain a deep understanding of the links between fractions, decimals and percentages so they can convert fluently between those most commonly seen in real-life.

- Represent fractions \& decimals on a number line
- Convert fluently between fractions decimals \& percentages
- Use \& interpret basic pie charts
- Identify and use simple equivalent fractions


## Assessment

End of Term 2 - In class, 45 minute assessment all Term 1 \& 2 topics.

| Misconceptions | Key Vocabulary | Knowledge Tracking |
| :---: | :---: | :---: |
| Seeing a digit as a number in its own right and not as a quantity where the value of each digit is determined by its place value | Convert <br> Decimal <br> Denominator <br> Equivalent <br> Improper <br> Integer <br> Interval <br> Median <br> Mixed number <br> Numerator <br> Range <br> Round <br> Significant figure | Already Seen: <br> In KS2, students will have covered place value extensively and the FDP equivalence. <br> The have not seen the range or median (only the mean). <br> To Build Towards: <br> This knowledge underpins a vast range of topics. <br> Year 7 Term 4 - Calculating with fractions. |
| Believing that fractions can be converted into decimals by essentially taking the numerator \& denominator and just squidging them together separated by a decimal point. <br> Students often consider percentages to be limited to $100 \%$. <br> The value of the frequency being used as the value of the angle in a Pie Chart. |  |  |

## Topics \&t <br> Substantive Knowledge

## Addition and Subtraction

The focus of this topic is building on the formal methods of addition and subtraction students have developed at Key Stage 2. Students will look at this in the context of interpreting and solving problems involving perimeter, money, bar charts and tables.

- Use formal written methods, applied to positive integers and decimals
- Solve problems in the context of perimeter, financial maths, tables, bar charts and frequency trees
- Add and subtract numbers in standard form (H)


## Multiplication and Division

This topic focuses on multiplication \& division. Students will understand how to form \& solve two-step equations, convert units \& solve problems in the context of perimeter \& area.

- Use formal written methods, applied to positive integers \& decimals
- Understand and use factors and multiples
- Convert metric units
- Understand \& use order of operations
- Solve problems involving area \& perimeter of 2D shapes
- Solve problems using the mean
- Explore multiplication and division in algebraic expressions


## Fractions and Percentages of amounts

This block focuses on the key concept of working out fractions and percentages of quantities and the links between the two.

- Find fractions of amounts
- Find a percentage of an amount using both mental methods and a calculator


## Assessment

End of Term 3 - In class, 45 minute assessment on the three Term 3 blocks of learning.

| Misconceptions | Key Vocabulary | Knowledge Tracking |
| :---: | :---: | :---: |
| Wrong place values used when adding or subtracting | Area <br> Average <br> Convert <br> Denominator <br> Equivalent <br> Factors <br> Mean <br> Multiples <br> Numerator <br> Parallel <br> Parallelogram <br> Perpendicular | Already Seen: <br> KS2 - formal methods of addition/ subtraction of integers and decimals. Understanding of perimeter. <br> To Build Towards: Y8 Term 4 - Standard Form |
| Believing that multiplication makes it bigger and dividing make it smaller. | Trapezium | Already Seen: <br> KS2 - multiplication/division of integers and decimals. Area of basic 2D shapes. Understanding of the mean, basic order of operations etc. <br> To Build Towards: Yr8 Term 3 - Further algebra. |
| Not putting brackets around negative numbers when squaring them on a calculator |  | Already Seen: <br> KS2 - non-calculator methods for fraction \& \% of an amount. <br> To Build Towards: <br> Y8 Term 4 - Multipliers for percentages, finding the original. |

## Topics \&t <br> Substantive Knowledge

## Operations \& Equations with Directed Number

This block is designed to extend and deepen the students understanding of directed number as they will have limited experience of this from primary school.

- Use the four operations, including formal written methods, applied to integers, positive and negative
- Use square and square roots (incl. the use of a calculator to calculate results)
- Substitute numerical values into formulae and expressions
- Understand and use the concepts and vocabulary of expressions, equations, inequalities, terms and factors
- Simplify and manipulate algebraic expressions to maintain equivalence


## Adding and Subtracting Fractions

This block builds on the Autumn term study of "key" fractions, decimals and percentages. It will provide more experience of equivalence of fractions with any denominator, and to introduce the addition and subtract of fractions.

- Convert Fractions, Decimals \& Percentages
- Express one quantity as a fraction of another, where the fraction is $<1$ and $>11$
- Order positive and negative integers, decimals and fractions


## Assessment

End of Term 4 - In class, 45 minute assessment all Term 3 \& 4 topics.

| Misconceptions | Key Vocabulary | Knowledge Tracking |
| :---: | :---: | :---: |
| Meaning behind negative numbers and consideration to when two negatives equal a positive. | Ascending Commutative Denominator Descending Evaluate Expression Inverse Numerator Product Solve Substitute | Already Seen: <br> KS2 - interpret negative numbers in context, count forwards and backwards with positive and negative numbers and calculate intervals across zero. Using the number line, pupils use, add and subtract positive and negative integers for measures such as temperature. <br> Year 7 Term 1 - Substitution and solving equations with positive numbers. <br> To Build Towards: <br> Year 8 Term 1 - Mixed Fractions <br> Year 8 Term 4 - Order of Operations <br> Year 9 Term 3 - Fraction Arithmetic |
| Common denominators are needed to add and subtract fractions. |  |  |

## Topics $\subset$ t <br> Substantive Knowledge

## Construction, measurement \& notation

Students will build on their KS2 skills using rulers and protractors to construct and measure increasingly complex diagrams:

- Draw and measure angles and triangles
- Identify types of triangles and polygons using appropriate mathematical language
- Construct and interpret Pie Charts


## Geometric reasoning

This topic covers basic geometric language, names and properties of types of triangles and quadrilaterals and the names of other polygons:

- Apply angle facts to solve problems involving angles in: straight lines, around a point, in a triangle, in quadrilaterals and in parallel lines.
- Derive and use the sum of angles in a triangle and use it to deduce the angle sum in any polygon.


## Developing number sense

Using mental strategies on using a known fact to find other facts:

- Employ decimals, fractions, powers and roots to solve problems.
- Begin to reason deductively using number and algebra


## Sets and probability

Students will learn about Sets, Set notation \& probability:

- Use appropriate language of probability and use the probability scale of 0 to 1 to solve problems.
- Construct and interpret Venn diagrams


## Prime numbers and proof

Revisit factors and multiples to introduce the concept of Prime numbers:

- Use factor knowledge to identify Prime Numbers
- Forming and testing conjectures

| Assessment | Misconceptions |
| :--- | :--- |

End of Term 5 - In class, 45 minute assessment on the two Term 5 blocks of learning. protractor.

End of Term 6 - End of Year assessment on all Year 7 topics. In class 45 minutes.

Distinguishing between Hatch Marks to identify equality and Arrows to identify parallel lines.

Adding all angles on the same line together even if they are in different places.

When multiplying two numbers, thinking that halving each number and then multiplying is equivalent rather than halving one and doubling the other one

## Key Vocabulary

## Knowledge Tracking

## Frequency <br> Already Seen:

 ParallelPerpendicular
Regular
Vertex Lack of understanding of the Venn Diagram and particularly the intersect section.

KS2 - use of ruler and protractor
To Build Towards:
Year 9 Term 2 - Constructions

## Already Seen

KS2 - properties of key 2D shapes, basic angle facts

## To Build Towards:

Year 9 Term 2 - Constructions

## Already Seen:

Building on a range of Year 7 knowledge

To Build Towards:
A golden thread through multiple topics

Already Seen:
N/A
To Build Towards:
Year 8 Term 6 - Probability

## Already Seen

Year 7 Term 3 - Factors/Multiples

## o Build Towards:

Year 9 Term 3 - Prime Factorisation

